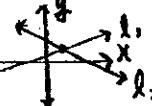


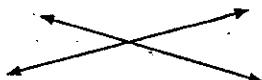
## IB Math 2: Relationship between Lines

Name: \_\_\_\_\_ Period: \_\_\_\_\_

**2-Dimensions** ( $l_1 : A_1x + B_1y = C_1$  and  $l_2 : A_2x + B_2y = C_2$ )

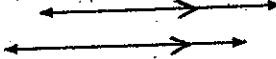


**Intersecting – Unique Solution**



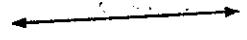
$$\frac{A_1}{A_2} \neq \frac{B_1}{B_2} \text{ OR } \frac{A_1}{B_1} \neq \frac{A_2}{B_2}$$

**Parallel- No Solution**



$$\frac{A_1}{A_2} = \frac{B_1}{B_2} \neq \frac{C_1}{C_2}$$

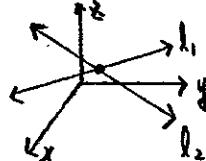
**Coincident – Infinitely many solution**



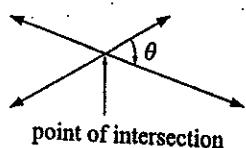
$$\frac{A_1}{A_2} = \frac{B_1}{B_2} = \frac{C_1}{C_2}$$

**3-Dimensions**  $l_1: \begin{cases} x = a_1 + x_1t \\ y = b_1 + y_1t \\ z = c_1 + z_1t \end{cases}$  and  $l_2: \begin{cases} x = a_2 + x_2\lambda \\ y = b_2 + y_2\lambda \\ z = c_2 + z_2\lambda \end{cases}$

$$\begin{cases} x = a_2 + x_2\lambda \\ y = b_2 + y_2\lambda \\ z = c_2 + z_2\lambda \end{cases}$$



**Intersecting – Unique Solution (coplanar)**



$$\begin{pmatrix} x_1 \\ y_1 \\ z_1 \end{pmatrix} \neq k \begin{pmatrix} x_2 \\ y_2 \\ z_2 \end{pmatrix} \Rightarrow$$

Find the intersection by solving  $l_1 = l_2$

(Three pairs' coordinates are coincident)

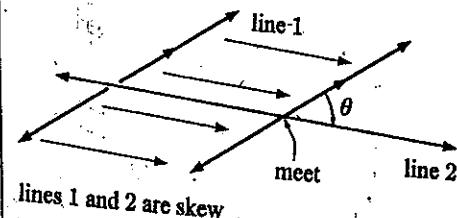
**Parallel- No Solution (coplanar)**

$$\begin{pmatrix} x_1 \\ y_1 \\ z_1 \end{pmatrix} = k \begin{pmatrix} x_2 \\ y_2 \\ z_2 \end{pmatrix}$$

**Coincident – Infinitely many solution (coplanar)**

$$\begin{pmatrix} x_1 \\ y_1 \\ z_1 \end{pmatrix} = k \begin{pmatrix} x_2 \\ y_2 \\ z_2 \end{pmatrix} \text{ and } \begin{pmatrix} a_1 \\ b_1 \\ c_1 \end{pmatrix} = k \begin{pmatrix} a_2 \\ b_2 \\ c_2 \end{pmatrix}$$

**Skewed -No solution (not coplanar)**



$$\begin{pmatrix} x_1 \\ y_1 \\ z_1 \end{pmatrix} \neq k \begin{pmatrix} x_2 \\ y_2 \\ z_2 \end{pmatrix} \Rightarrow$$

Show skewed by solving  $l_1 = l_2$

(Two pairs' coordinates are coincident but one pair is not equal)

Classify the following line pairs as intersecting, slew, or parallel.

a.  $l_1; \begin{cases} x = 1 + 3t \\ y = -2 - 2t \end{cases}$  and  $l_2; x = 2 - y = z + 2$   
 $z = 0.5 + 2t$

b.  $l_1; r = (1i + 2j + 3k) + (1i - j + 2)\lambda$  and  $l_2; \frac{x-2}{3} = \frac{3-y}{2} = z + 5$

c.  $l_1; r = (1i + 8j + 5k) + (2i - j + 3)\lambda$  and  $l_2; \frac{2-x}{4} = \frac{y+1}{2} = \frac{4-z}{6}$