

IB Math 1 2B Function Notation

Relation: Any relationship between two variables.

Function: A relation in which each input has only one output.

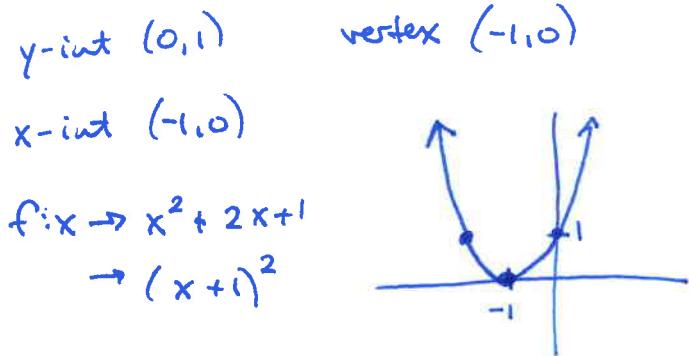
Function Notation

$$f(x)$$

$$f : x \rightarrow$$

$$f : x \rightarrow x^2 + 2x + 1$$

1. Sketch a graph.



Domain: $(-\infty, \infty)$

all real numbers

\mathbb{R}

Range: $[0, \infty)$

$$\underline{x = -3, 1}$$

$$\begin{aligned} y &\geq 0 \\ [0, \infty[\end{aligned}$$

2. Find x when $f(x) = 4$

$$\begin{aligned} f(x) &= x^2 + 2x + 1 & 4 &= (x+1)^2 \\ 4 &= x^2 + 2x + 1 & \pm 2 &= x+1 \\ 0 &= x^2 + 2x - 3 & x+1 &= 2 \quad x+1 = -2 \\ 0 &= (x+3)(x-1) & x &= 1, \quad x = -3 \end{aligned}$$

3. Evaluate and simplify

a. $f(3a)$

$$f(x) = x^2 + 2x + 1$$

$$\begin{aligned} f(3a) &= (3a)^2 + 2(3a) + 1 \\ &= \underline{\underline{9a^2 + 6a + 1}} \end{aligned}$$

b. $f(a+3)$

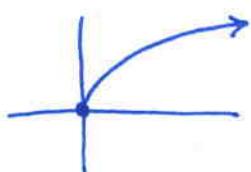
$$f(x) = x^2 + 2x + 1$$

$$\begin{aligned} f(a+3) &= (a+3)^2 + 2(a+3) + 1 \\ &= a^2 + 6a + 9 + 2a + 6 + 1 \\ &= \underline{\underline{a^2 + 8a + 16}} \end{aligned}$$

2C Domain and Range

Find the Domain and Range of each function.

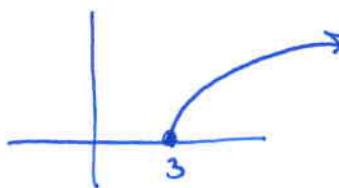
$$1. f(x) = \sqrt{x}$$



$$D: [0, \infty)$$

$$R: [0, \infty)$$

$$2. g(x) = \sqrt{x-3}$$



$$D: [3, \infty)$$

$$R: [0, \infty)$$

must be 0 or greater

$$x-3 \geq 0$$

$$x \geq 3$$

$$3. h(x) = 2 + \sqrt{5 - 3x}$$

0 or more

$$5 - 3x \geq 0$$

$$D: (-\infty, \frac{5}{3}]$$

$$-3x \geq -5$$

$$R: [2, \infty)$$

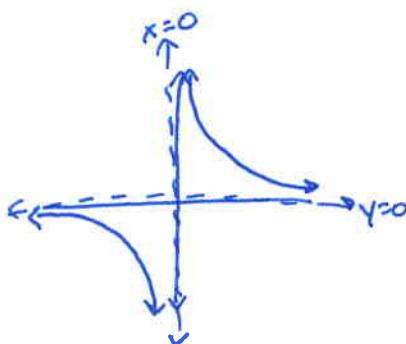
$$x \leq \frac{5}{3}$$

$$4. j(x) = \frac{1}{x+4}$$

$$D: (-\infty, -4) \cup (-4, \infty) \quad R, x \neq -4$$

$$R: (-\infty, 0) \cup (0, \infty) \quad R, y \neq 0$$

$$y = \frac{1}{x}$$



$$D: (-\infty, 0) \cup (0, \infty)$$

$$R, x \neq 0$$

$$\left\{ x \in \mathbb{R} \mid x \neq 0 \right\} \text{ super branch}$$

$$5. k(x) = -4 + \frac{5}{x^2 - 36}$$

$$R: (-\infty, 0) \cup (0, \infty)$$

$$x^2 - 36 = 0 \quad D: (-\infty, -6) \cup (-6, 6) \cup (6, \infty)$$

$$x = 6, -6 \quad R, x \neq -6, 6$$

$$R: (-\infty, -4) \cup (-4, \infty) \xrightarrow{\text{HW}} 2B (3-5 \text{ odd letters}, 6-12)$$

$$2C (1-3, 4cefikl, 5abc)$$