

Continuity

Notes

Defining Continuity:

★ A function f is continuous at a point $x=c$ if

(1) $f(c)$ is defined.

(2) $\lim_{x \rightarrow c} f(x)$ exists $(\lim_{x \rightarrow c^+} f(x) = \lim_{x \rightarrow c^-} f(x))$

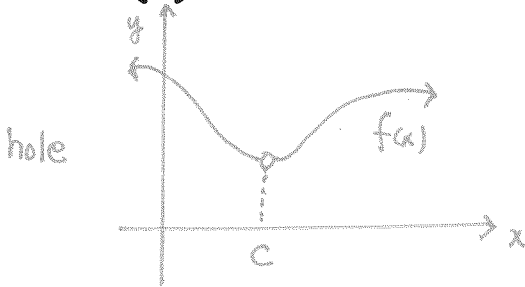
(right-hand-side and left-hand-side)

(3) $\lim_{x \rightarrow c} f(x) = f(c)$

Notes

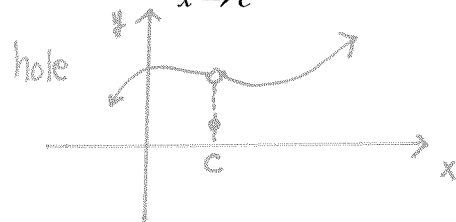
Discontinuity

a. $f(c)$ is undefined

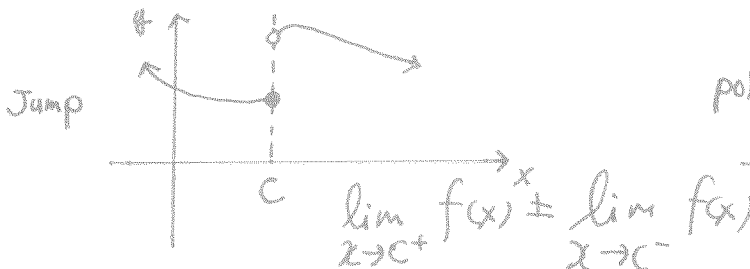


b. $f(c)$ is defined

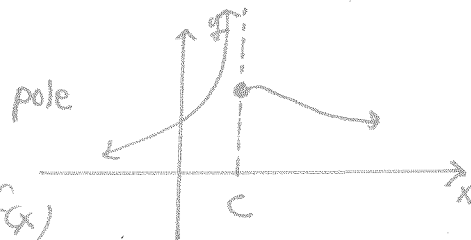
but, $\lim_{x \rightarrow c} f(x) \neq f(c)$



c. $\lim_{x \rightarrow c} f(x) \neq f(c)$



d. $\lim_{x \rightarrow c^-} f(x) = +\infty$ $\lim_{x \rightarrow c^+} f(x) = f(c)$



e. $\lim_{x \rightarrow c^+} f(x) = +\infty$ $\lim_{x \rightarrow c^-} f(x) = +\infty$

