

$$\frac{dp}{dt} = kp \left(1 - \frac{p}{4000}\right) \Rightarrow \int \frac{dp}{p \left(1 - \frac{p}{4000}\right)} = \int k dt$$

$$\left(\begin{aligned} \frac{A}{p} + \frac{B}{1 - \frac{p}{4000}} &= 1 \\ A \left(1 - \frac{p}{4000}\right) + Bp &= 1 \\ A \neq 1 \quad p = \frac{1}{4000} \end{aligned} \right)$$

$$\Rightarrow \int \left(\frac{1}{p} + \frac{\frac{1}{4000}}{1 - \frac{p}{4000}} \right) dp = kt + C$$

$$\Rightarrow \int \left(\frac{1}{p} + \frac{1}{4000-p} \right) dp = kt + C$$

$$\Rightarrow \ln p - \ln(4000-p) = kt + C$$

$$\Rightarrow \ln \left(\frac{p}{4000-p} \right) = kt + C$$

$$\Rightarrow e^{kt} \cdot A = \frac{p}{4000-p}$$

$$\Rightarrow p = e^{kt} \cdot A (4000-p)$$

$$p(1 + e^{kt}) = A \cdot 4000 \Rightarrow p = \frac{4000}{A_0 e^{-kt} + 1}$$

$$(t=0, p=40)$$

$$40 = \frac{4000}{A_0 e^{-k(0)} + 1}$$

$$A_0 = \frac{4000}{40} - 1$$

$$A_0 = 99$$

$$p = \frac{4000}{99 A^{-kt} + 1}$$

$$(t=5, p=104)$$

$$104 = \frac{4000}{99 A^{-k(5)} + 1}$$

$$104(99 A^{-5k} + 1) = 4000$$

$$99^{-5k} + 1 = \frac{4000}{104}$$

$$(-5k) \ln 99 = \ln \left(\frac{4000}{104} - 1 \right)$$

$$k \approx -0.194$$

$$t=15$$

$$p = \frac{4000}{99 A^{1.194 \times 15} + 1}$$

$$p \approx 626$$