

IB Calculus Exit Slip

Name: Key

The region M is enclosed by the function  $y = x^2$  and  $y = 3x$ .

- a. Sketch the solid generated by revolving M about the x-axis and set up the integral of the volume.

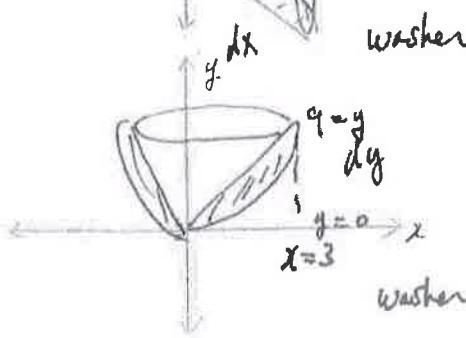
$$y = \sqrt{y} \quad x = \frac{y}{3}$$

$$R_{\text{outer}} = 3x$$

$$r_{\text{inner}} = x^2$$

$$V = \pi \int_0^3 ((3x)^2 - (x^2)^2) dx$$

- b. Sketch the solid generated by revolving M about the y-axis and set up the integral of the volume.

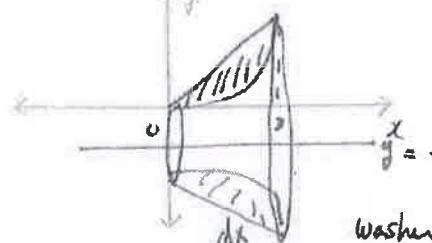


$$R_{\text{outer}} = \sqrt{y}$$

$$r_{\text{inner}} = \frac{y}{3}$$

$$V = \pi \int_0^9 ((\sqrt{y})^2 - (\frac{y}{3})^2) dy$$

- c. Sketch the solid generated by revolving M about  $y = -1$  and set up the integral of the volume.

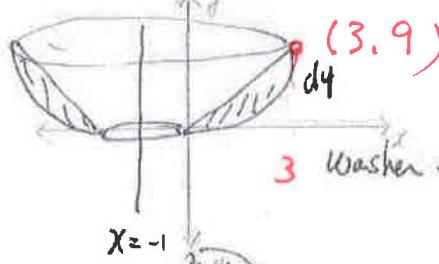


$$R_{\text{outer}} = 3x + 1$$

$$r_{\text{inner}} = x^2 + 1$$

$$V = \pi \int_0^3 ((3x+1)^2 - (x^2+1)^2) dx$$

- d. Sketch the solid generated by revolving M about  $x = -1$  and set up the integral of the volume.

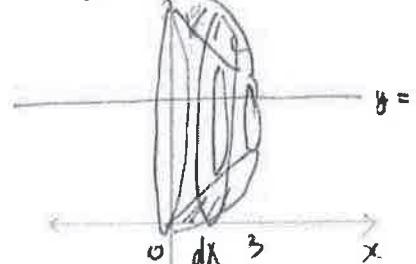


$$R_{\text{outer}} = \sqrt{y} + 1$$

$$r_{\text{inner}} = \frac{4}{3} + 1$$

$$V = \pi \int_0^9 ((\sqrt{y}+1)^2 - (\frac{4}{3}+1)^2) dy$$

- e. Sketch the solid generated by revolving M about  $y = 10$  and set up the integral of the volume.

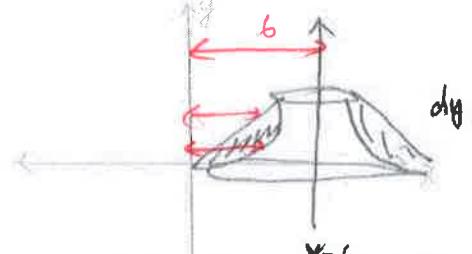


$$R_{\text{outer}} = 10 - x^2$$

$$r_{\text{inner}} = 10 - 3x$$

$$V = \pi \int_0^3 ((10-x^2)^2 - (10-3x)^2) dx$$

- f. Sketch the solid generated by revolving M about  $x = 6$  and set up the integral of the volume.



$$R_{\text{outer}} = 6 - \frac{y}{3}$$

$$r_{\text{inner}} = 6 - \sqrt{y}$$

$$V = \pi \int_0^9 ((6-\frac{y}{3})^2 - (6-\sqrt{y})^2) dy$$