

No Calculators!

1. Given $h(x) = \frac{(x-1)(x+2)}{(2x-1)}$

- a. Find the vertical asymptote(s)

$$x = \frac{1}{2}$$

- b. Find the oblique asymptote.

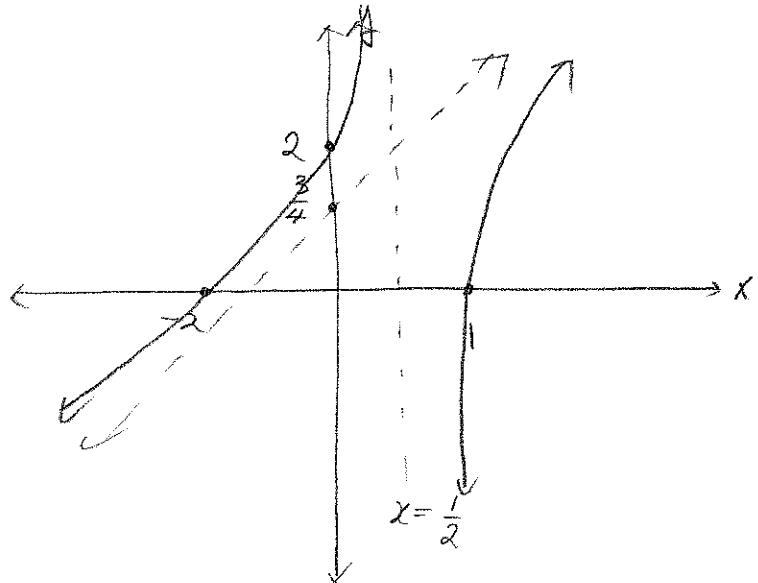
$$y = \frac{1}{2}x + \frac{3}{4}$$

- c. Find x-intercept(s) and y-intercept.

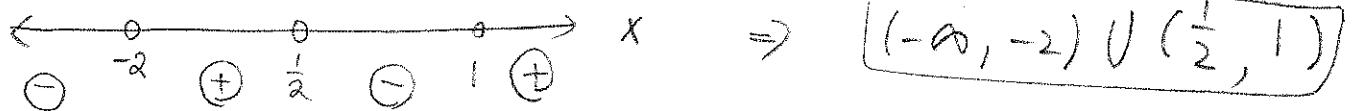
$$x: (-1, 0) \quad (2, 0)$$

$$y: (0, -2)$$

- d. Sketch the graph using the answers of a-c.



2. Make a sign diagram for $h(x) = \frac{(x-1)(x+2)}{(2x-1)}$ and then solve $\frac{(x-1)(x+2)}{(2x-1)} < 0$



3. For the function $f(x) = \frac{-6x^2 - 3x + 18}{2x^2 - 5x + 3}$ $= \frac{-3(2x+3)(x+2)}{(2x-3)(x-1)}$

- a) State the domain and the range.

$$D: \left\{ x \in \mathbb{R} \mid x \neq -\frac{3}{2}, x \neq 1 \right\} \quad R: \left\{ y \in \mathbb{R} \mid y \neq -3 \right\}$$

- b) Describe the end behaviors for $f(x)$ as $x \rightarrow \infty$ and $x \rightarrow -\infty$.

$$\text{as } x \rightarrow \infty, y \rightarrow -3$$

$$\text{as } x \rightarrow -\infty, y \rightarrow -3$$

$$H.A: y = -3$$

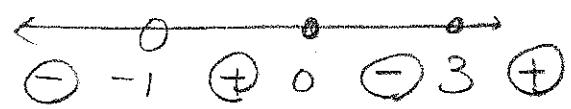
- c) Describe the transformation of $f(x)$ from $y = \frac{1}{x}$.

$$y = -3 + \frac{-9}{x-1} \Rightarrow \left(\begin{array}{l} \text{Vertical Dilation by Factor of 9} \\ \text{Reflection across } x=1 \end{array} \right) / \begin{array}{l} \text{H.T.: 1 unit Right} \\ \text{I.T.: 3 units down} \end{array}$$

4. Solve $\frac{3x-1}{x+1} \leq x-1$. Support your answers by sign diagram.

$$x \neq -1 \quad x = 0 \quad x = 3$$

$$\left. \begin{aligned} & \frac{3x-1}{x+1} - \frac{(x-1)(x+1)}{(x+1)} \leq 0 \\ & \frac{(3x-1) - (x^2-1)}{x+1} \leq 0 \\ & \frac{x(x-3)}{x+1} \geq 0 \end{aligned} \right\} \Rightarrow$$



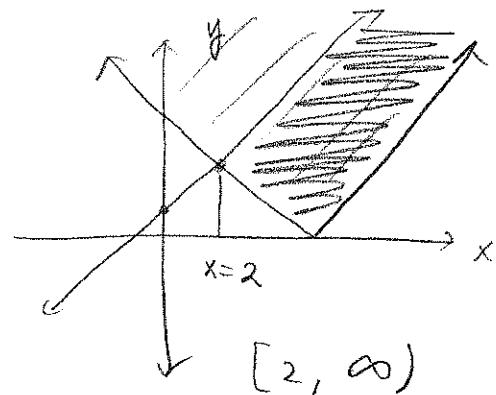
$$(-1, 0] \cup [3, \infty)$$

5. Given $|x-5| \leq x+1$

a) Solve analytically

b) Solve graphically (Use G calculator)

$$\begin{aligned} x > 5 & \quad x-5 \leq x+1 \Rightarrow R = x \\ & \quad -5 \leq 1 \\ & \Rightarrow x \geq 5 \quad \xrightarrow{\text{graph}} \quad \Rightarrow [5, \infty) \\ x < 5 & \quad -x+5 \leq x+1 \Rightarrow \\ & \quad x \geq 2 \quad \xrightarrow{\text{graph}} \end{aligned}$$

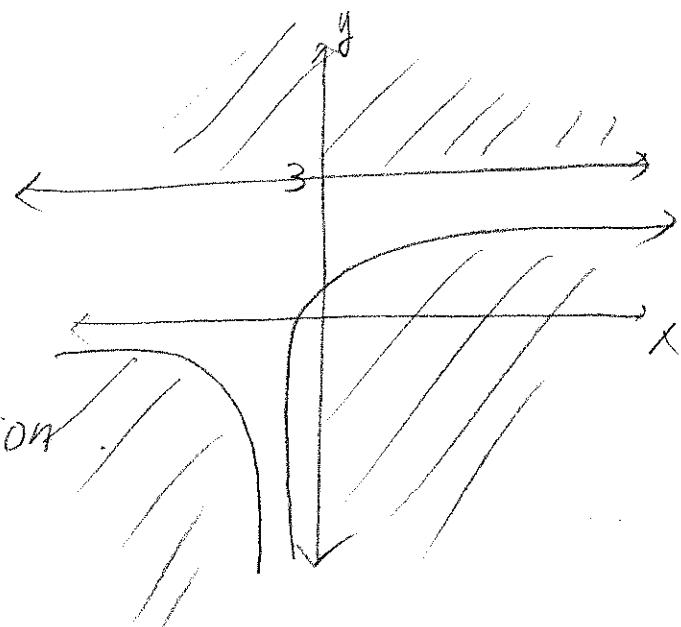


6. Given $\frac{2x+1}{|x+2|} > 3$

a) Solve analytically

b) Solve graphically (Use G calculator)

$$\begin{aligned} x < -2 & \Rightarrow 2x+1 > -3(x+2) \Rightarrow x > 1 \\ & \text{No solution} \quad \xrightarrow{\text{graph}} \\ x > -2 & \Rightarrow 2x+1 > 3(x+2) \\ & \quad x < -4 \\ & \quad \xrightarrow{\text{graph}} \quad \text{No solution} \end{aligned}$$



No Solution